Electron Affinities, Ionization Energies, and Fragmentation Energies of Fe*ⁿ* **Clusters** $(n = 2-6)$: A Density Functional Theory Study

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The electronic and geometrical structures of the ground and exited states of Fe_n, Fe_n⁻, and Fe_n⁺ are computed by density functional theory. Because the assignment of the ground states of Fe_3 , Fe_3^- , Fe_4 , and Fe_4^- is controversial, these systems are studied using several different functionals. It appears that the LSDA and B3LYP methods do not work well for iron clusters and should be avoided. The number of unpaired electrons in the neutral ground states is $6(F_{2})$, $10(F_{3})$, $14(F_{4})$, $16(F_{5})$, and $20(F_{6})$. The number of unpaired electrons in the ground states of the anions and cations differ by one from the corresponding neutral, except for Fe_4^+ , which has three fewer unpaired electrons than Fe₄. The computed DFT adiabatic electron affinities and ionization potentials of the neutral clusters are in good agreement with experiment. Fragmentation energies are in qualitative agreement with experiment, where the error is about 1 eV for the dissociation energy of the iron dimer. The natural bond analysis allows one to qualitatively understand the nature of high local magnetic moments at iron sites and their evolution from $Fe₂$ to $Fe₆$.

Introduction

Iron clusters have been found to act as catalysts for producing single-walled^{1,2} carbon nanotubes (SWNT), which are expected to possess unique mechanical, electronic, magnetic, and optical properties. Smalley with co-workers³ have developed a highpressure high-temperature process where $Fe(CO)$ ₅ decomposes and forms iron clusters.4 The latter catalyze the growth of SWNTs in the presence of a CO flow. Chemical vapor deposition techniques use CO or hydrocarbon feedstock and iron particles as a catalysist.⁵ When CO is used as a feedstock, by analogy6 with the Boudouard disproportionation reaction of producing atomic carbon from vibrationally excited carbon monoxide $CO(v) + CO(w) \rightarrow C + CO_2$, the critical step in the SWNT growth is believed to be due to $M-CO + CO \rightarrow M-C$ $+$ CO₂ (where M is a catalyst cluster) reactions. However, the mechanism of iron-catalyzed growth of SWNTs is not well understood; $7,8$ for example, the size and the charge of the catalytic metal particles are unknown.

Experimental spectroscopic data for iron clusters are rather scarce. The bond length appears to be measured only for $Fe₂$ trapped in argon ($r_e = 1.87 \pm 0.13 \text{ Å}$)⁹ and neon ($r_e = 2.02 \pm 0.13 \text{ Å}$)² 0.02 Å)¹⁰ matrixes. Vibrational frequencies were obtained for Fe₂ (299.6 cm⁻¹),¹¹ Fe₂⁻ (250 \pm 20 cm⁻¹),¹² and Fe₃.^{13,14} Nour
et al.¹³ assigned a band at 180 cm⁻¹ to the Fe₂ *y*₂ antisymmetric et al.¹³ assigned a band at 180 cm⁻¹ to the Fe₃ ν_3 antisymmetric stretching frequency, but a recent resonance Raman spectroscopy study by Moscovits with co-workers¹⁴ found that assignment of frequencies of Fe₃ is not straightforward "since the molecule does not have conventional asymmetric stretching and bending modes".

Electron affinities for clusters Fe_n up to $n = 34$ were measured^{15,16} using photoelectron spectroscopy while ionization energies of the clusters up to $n = 100$ were obtained¹⁷⁻¹⁹ using photoionization. Fragmentation energies of the Fe*ⁿ* ⁺ clusters up

to $n = 19$ were obtained²⁰⁻²⁴ using collision-induced dissociation (CID) of the clusters with xenon. Bond dissociation Fe*ⁿ*-¹ + Fe energies of the neutral clusters were derived from the experimental values of ionization energies of the neutrals and fragmentation data for the corresponding cations.25 Magnetic behavior of iron clusters is rather complicated.²⁶ A slow oscillating convergence of magnetic moments of Fe*ⁿ* in the range of $25 \le n \le 700$ to the bulk value of 2.15 μ **B** per atom has been observed in Stern-Gerlach deflection experiments.²⁷ The magnetic moment per atom for small iron clusters is larger $(2.7 -$ 3.3 μ_B)^{27,28} than those found for larger clusters or the bulk.

The ground state of Fe₂ has been the subject²⁹ of a great number of computations performed at different ab initio and density functional theory (DFT) levels. For larger clusters, we are aware of one ab initio study 30 based on configuration interaction (CI) single-point calculations at assumed or Hartree-Fock geometries. The spin multiplicities obtained in this study increase with the addition of each Fe atom by four from $7(F_{e_2})$ to 23(Fe₆). The remaining computations³¹⁻⁴⁶ on iron clusters up to $n = 19$ have been performed mainly using the local spin density approximation (LSDA) often combined with the use of effective core potentials (ECP). Beyond the LSDA, Salahub et al*.* ³⁴ used LSDA with so-called nonlocal gradient corrections (LSDA-NL) for the neutral, anionic, and cationic iron clusters up to $n = 5$. The number of unpaired electrons, 2S (where S is the net spin), was found^{34,36,37} to be 6(Fe₂), 8(Fe₃), 12(Fe₄), 16- $(Fe₅)$, and $20(Fe₆)$. This is in disagreement with the more recent DFT with a generalized gradient approximation for the exchangecorrelation potential (DFT-GGA) computations, $32,40$ which have predicted 10 unpaired electrons for Fe₃ and 14 for Fe₄. Using a Discrete Variational X_α method, Cheng and Ellis obtained³³ an even larger *2S* value of 16 for Fe4.

The most recent paper of Salahub and Chrétien,⁴⁷ published while the present work was in preparation, reported the results of calculations of Fe_n, Fe_n⁻, and Fe_n⁺ ($n = 1-4$) using DFT-
GGA methods. They also obtained 10 and 14 unpaired electrons GGA methods. They also obtained 10 and 14 unpaired electrons for $Fe₃$ and for $Fe₄$, respectively. For $Fe₃⁻$ and $Fe₄$ they found

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the ground states to be $^{12}B_1$ and $^{15}A''$, respectively, which is in agreement with the previous DFT-GGA work.40,42 However, for Fe₃ they found an $^{11}A_2$ ground state, and an $^{11}A_1$ state, which previously40 was assigned as the ground state, was found to be a transition state.

The purpose of this work is to determine the ground states and their geometrical structures of small Fe clusters, namely Fe_n, Fe_n⁻, and Fe_n⁺ ($n = 2-6$). We also report their vibrational
frequencies and infrared intensities as this may aid in the frequencies and infrared intensities, as this may aid in the interpretation of future experimental work. Because this work will act as a building block for future studies of the chemistry of Fe clusters, it is important to calibrate our calculations against experiment, which consists mainly of the electron affinities, ionization energies, and fragmentation energies. While our main interest is the electronic and geometric structure of these clusters, previous work has shown some variation in results with choice of function, and therefore, we test the performance of several DFT-GGA approaches to establish the functional of choice for this class of systems.

Computational Details

We performed density-functional theory⁴⁸ calculations using several different functionals. Our primary exchange-correlation functional consisted of the combination of Becke's exchange⁴⁹ and Perdew-Wang's correlation functionals,⁵⁰ referred to as BPW91. For Fe₃ and Fe₄, several additional functionals are used, namely LSDA (Slater's exchange⁵¹ and Vosko-Wilk-Nusair's correlation⁵²), hybrid B3LYP,^{53,54} BLYP (Becke's exchange⁴⁹ and Lee-Yang-Parr's correlation⁵⁵), BP86 (Becke's exchange⁴⁹ and Perdew's correlation⁵⁶), BPBE (Becke's exchange⁴⁹ and Perdew-Burke-Ernzerhof's correlation⁵⁷), and PBEPBE (Perdew-Burke-Ernzerhof's exchange and correlation⁵⁷).

The Gaussian 98 program⁵⁸ was used for all calculations. The 6-311+G* (15s11p6d1f)/[10s7p4d1f] basis set⁵⁹⁻⁶¹ was used. Calibration computations⁶² were performed for $Fe₂$ with the recently developed⁶³ triple-ζ (TZ) correlation consistent basis set. The results obtained using the larger TZ basis set for the Fe₂ ground ⁷ Δ _u state (r_e = 2.00 Å and ω_e = 404 cm⁻¹) are only marginally different from those obtained with the 6-311+G* basis ($r_e = 2.01$ Å and $\omega_e = 397$ cm⁻¹). Thus, we conclude that expanding the basis set will not significantly affect the results. However, as we discuss below, the results depend somewhat on the choice of functional.

The geometry of each species was optimized for each possible spin multiplicity until further increasing the spin multiplicity would result in a state whose total energy is above the energy of the lowest asymptote. Subsequent frequency calculations were performed using analytical second derivatives to confirm that the optimized geometries correspond to minima. Our reported electron affinities and ionization energies correspond to adiabatic values, that is, they are computed as differences in total energies of the corresponding species, each at its equilibrium geometry. The values are corrected for the zero point energies (ZPEs), where the ZPEs are computed as one-half the sum of the vibrational frequencies. Fragmentation energies are also corrected for the ZPEs. To gain insight into the nature of chemical bonding in iron clusters, we have performed Natural Bond orbital Analysis.64,65

Results and Discussion

Iron Dimer. The ground state of iron atom is ⁵D and corresponds to a $4s²3d⁶$ occupation. In the Fe₂ dimer, one or two 4s electrons are promoted into the 3d-manifold. If one 4s electron is promoted, then so-called mixed states are formed

Figure 1. Bonding patterns of ground-state Fe_2 , Fe_2^- , and Fe_2^+ .

(the asymptote is $4s^23d^6 + 4s^13d^7$). The lowest mixed state is ${}^{9}\Sigma_{g}^{-}$, which is found to be the ground state in recent^{66,67} multireference CI (MRCI) calculations. If both 4s electrons are promoted (the asymptote is $4s^13d^7 + 4s^13d^7$), the lowest state is ${}^{7}\Delta_{u}$, which is identified as the ground state in DFT studies²⁹ and some ab initio methods.30 The difference between these two states is best seen by using the NBO analysis. This analysis operates with localized (Lewis) bonding orbitals, which appear to be well suited for describing the chemical bonding of the 3d metal dimers. The NBO orbitals can be identified as bonding $(4s + 4s)$, $(3d_{\sigma} + 3d_{\sigma})$ (or hybridized $(3d_{\sigma}4s + 3d_{\sigma}4s)$), $(3d_{\pi} +$ $3d_{\pi}$), and $(3d_{\delta} + 3d_{\delta})$ or as the corresponding antibonding orbitals in each spin representation. Note that occupation of a bonding-antibonding pair of the same type results in two localized spin-orbitals (LSO) of a pure atomic character.⁶⁸

The bonding pattern⁶⁹ of the ⁷∆_u (4s¹3d⁷ + 4s¹3d⁷) state is presented in Figure 1. As can be seen, the 4s electrons occupy a two-electron $(4s + 4s)$ bond, while the four spin down 3d electrons fill the four lowest-energy bonding orbitals. Ten spinup 3d electrons are chemically inactive and occupy the LSOs. The bottom panel of Figure 1 presents the bonding pattern of the ground ${}^8\Delta_g$ state of Fe₂⁻. An extra electron attaches to the spin-up $4s-4s$ antibonding orbital of Fe₂ that destroys the spin up $4s + 4s$ bond and creates two $4s$ LSOs, while the spindown part of the $4s + 4s$ bond remains the same. The bonding pattern in the mixed ${}^{9}\Sigma_{g}^{-}$ state of Fe₂ is the same as ${}^{8}\Delta_{g}$ state of Fe₂⁻, except $(3d_δ + 3d_δ)$ orbital is empty in the ⁹ Σ_g^- state.

At the DFT level, the additional 0.87 eV $4s \rightarrow 3d$ promotion energy⁷⁰ for the ${}^{7}\Delta_{u}$ state has been compensated for by the energy gained due to the formation of two one-electron bonds in the ${}^{7}\Delta_{u}$ state with respect to those in the ${}^{9}\Sigma_{g}^{-}$ state. While the BPW91 favors the bond formation and places ${}^{7}\Delta_{u}$ below ${}^{9}\Sigma_{g}^{-}$ by 0.51 eV (similar values were obtained using other functionals, see Table 1), the MRCI methods predict^{66,67} opposite order for these two states.

In the ground ${}^8\Delta_u$ state of Fe₂⁺, the electron formally leaves the $(4s+4s)$ bonding orbital of Fe₂. However, the nearly pure

TABLE 1: Different States of Fe₂, Fe₂⁻, and Fe₂⁺ Computed at the BPW91 and PP86 Levels*^a*

		BPW91		PP86 ^b		
state	ΔE , eV	$r_{\rm e}$, $\rm \AA$	$\omega_{\rm e}$, cm ⁻¹	ΔE , eV	r _e , Å	$\omega_{\rm e}$, cm ⁻¹
			Fe ₂			
$^7\Delta$ _u	0.00	2.011	397	0.00	2.008	415
$^{9}\Delta_{g}$	$+0.48$	2.256	279			
$\frac{{}^{9}\Sigma_{g}^{0}}{{}^{7}\Delta_{g}}$ $\frac{{}^{9}\Delta_{g}}{{}^{9}\Delta_{u}}$	$+0.51$	2.152	331	$+0.53$	2.151	332
	$+0.65$	2.103	366			
	$+0.84$	2.356	256			
$5\Sigma_{\rm g}$ -	$+0.84$	1.834	476	$+0.84$	1.860	510
			Fe ₂			
	-0.94	2.071	351	-1.17	2.073	358
$\overset{8\Delta_g}{\circ}\Delta_g$	-0.53	2.051	361	-0.84	2.050	370
$8\Delta_u$	-0.34	2.174	315			
$6\Sigma_{\rm u}$ -	-0.09	1.879	423			
			$Fe2$ ⁺			
${}^8\Delta_{\rm n}$	$+6.68$	2.172	319	$+7.14$	2.180	319
${}^8\Delta_g$	$+7.08$	2.264	290	$+7.50$	2.271	296
$6\Delta_{g}$	$+7.95$	1.946	416	$+7.94$	1.949	454
${}^6\Delta_u$	$+7.96$	2.081	350			
$^{10}\Sigma_{\rm g}$	$+8.00$	2.360	243	$+8.51$	2.373	240

^a Total energy shifts (∆*E*) are given with respect to the ground state of Fe₂. Experiment: Fe₂, $r_e = 2.02 \pm 0.02 \text{ Å}^{10} \omega_e = 299.6 \text{ cm}^{-1}$;¹¹
Fe₂ $\omega_e = 250 + 20 \text{ cm}^{-1}$ (ref 12) ^b Ref 47 $Fe₂⁻$, $\omega_e = 250 \pm 20$ cm⁻¹ (ref 12). *b* Ref. 47.

 $(3d_{\sigma} + 3d_{\sigma})$ orbital of Fe₂ becomes a strongly mixed $(3d_{\sigma}4s +$ $3d_{\sigma}4s$) orbital in Fe₂⁺, see Figure 1.

Table 1 presents the spectroscopic constants of the ground and some excited states of Fe_2 , Fe_2^- , and Fe_2^+ . They are compared to those obtained recently by Salahub and Chrétien⁴⁷ at the PP86 level. The available experimental results for the ground states of $Fe₂$ and $Fe₂⁻$ are in reasonable agreement with the theory, although the differences in vibrational frequencies appear to be rather large. This is somewhat puzzling, since the $Fe-Fe$ frequency computed for $Fe₂CO$ at the BPW91/ 6-311+ G^* level is in much better agreement with experiment⁷¹ (the difference is about 40 cm⁻¹). The same behavior is observed for the Co-Co frequencies in $Co₂$ and $Co₂CO$; while the BPW91 frequency⁶⁸ of Co₂ is about 100 cm⁻¹ higher than the experimental value, the discrepancy⁷² is reduced to 11 cm⁻¹ in Co₂CO.

Ground State of the Iron Trimer. The first DFT-GGA study⁴⁰ predicted an ${}^{11}A_1$ ground state of Fe₃, while the more recent work of Salahub and Chrétien⁴⁷ predicts an $^{11}A_2$ ground state and that the ${}^{11}A_1$ state is not even a minimum. Therefore, we first study these two states, as well as the lowest ${}^{11}B_1$ and $11B₂$ states, in detail. To answer if the ground state depends on

the choice of functional, we study these four states using several functionals. In additional to the variation with functional, we compute the frequencies with the standard (the integration grid is FINE) and tight (Opt=TIGHT, Grid=UltraFINE) options, because it is known⁷³ that molecular properties, especially vibrational frequency, may strongly be influenced by the accuracy of the integration.

At all levels of theory used, the $^{11}A_1$ and $^{11}A_2$ states are nearly degenerate in total energy. For all of the functionals used in this work, the $^{11}A_1$ is a minimum, which contradicts the result of Salahub and Chrétien,⁴⁷ who found the ¹¹A₁ to be a transition state. The $^{11}A_2$ state is a minimum for all functionals, except BLYP. As shown in Table 2, the ${}^{11}A_2$ state is the ground state at the BPW91, BP86, BPBE, and PP86 levels. The PBEPBE approach predicts the $^{11}A_2$ state to be degenerate in total energy with the ¹¹ A_1 state (see Table 3) and places the ¹¹ A_1 state slightly below (by 0.004 eV) if the tight option is used. The BLYP level predicts the $^{11}A_2$ state to be a transition state. Note that the choice of grid affects the lowest frequency which decreases with respect to that computed using the standard (FINE) integration option. The largest computed separation between the $^{11}A_2$ and $^{11}A_1$ states is $+0.012$ eV, which is obtained at the BPBE level. Because such a small difference is beyond the accuracy of the current computations, one may conclude that higher levels of theory are required for an assignment of ${}^{11}A_1$ or ${}^{11}A_2$ as the ground state of Fe3.

Table 4 shows that the $^{11}B_2$ state is above the $^{11}A_2$ state by 0.17-0.19 eV. Again, only the BLYP level predicts this state to be a transition state. The BLYP predicts the ${}^{11}B_1$ state to be a minimum, while the BPW91 and BPBE predict this state to be a transition state in computations performed with the standard grid. The BP86 and PBEPBE levels require a tighter integration to arrive at the same conclusion. The PP86 level produces the bond lengths and vibrational frequencies, which are close to those obtained at the BLYP level, and also predicts the $^{11}B_1$ state to be a minimum. While four levels, BPW91, BP86, BPBE, and PBEPBE, provide similar results, the BPW91 frequencies appear to be less sensitive to the integration quality. In addition to the differences in functionals used, our results suggest that some of the disagreement between our results and those of Salahub and $Chrétien^{47}$ may be due to the grid used. We should also note that some differences could arise from their computation of the vibrational frequencies by finite differences compared with our use of analytical second derivatives.

Note that all three stable states found have the $Fe₂Fe₁Fe₃$ angle less than 60°, which is expected to enhance the bonding between

TABLE 2: ¹¹A₂ State of Fe₃ Computed Using the BPW91, BLYP, BP86, BPBE, PBEPBE (Using Two Sample Grids for **Integrating Exchange-Correlation Energy Contribution), and PP86 Levels***^a*

method	ΔE_{tot} eV	$R_{1,2;1,3}$ Å	$R_{2,3}$ Å	$\angle 213^\circ$	ω (b ₂)cm ⁻¹	$\omega(a_1)$ cm ⁻¹	ω (a ₁) cm ⁻¹
					$^{11}A_2$ (α : $a_1-a_2-b_1-b_2$ β : $a_1-a_2-b_1-b_2$) (19-5-7-13 15-3-6-10) Grid = FINE		
BPW91	0.0	2.303	2.166	56.1	56	232	354
BLYP	$+0.004$	2.324	2.188	56.2	58i	227	341
BP86	0.0	2.296	2.162	56.2	29	234	357
BPBE	0.0	2.300	2.165	56.1	60	233	355
PBEPBE	0.0	2.301	2.171	56.3	31	234	352
PP86	0.0	2.313	2.176	56.1	56	235	347
				$^{11}A_2$ (19-5-7-13 15-3-6-10) Grid = UltraFINE			
BPW91	0.0	2.301	2.167	56.1	48	231	352
BLYP	$+0.003$	2.323	2.189	56.2	68i	225	339
BP86	0.0	2.295	2.164	56.2		233	354
BPBE	0.0	2.300	2.166	56.1	53	231	352
PBEPBE	$+0.004$	2.300	2.172	56.3	15	233	350

^a The PP86 results are from ref 47. Total energy shifts (∆*E*) are given with respect to the lowest energy state obtained by the corresponding method and grid.

TABLE 3: 11A1 State of Fe3 Computed Using the BPW91, BLYP, BP86, BPBE, PBEPBE (Using Two Sample Grids for Integrating Exchange-Correlation Energy Contribution), and PP86 Levels*^a*

method	$\Delta E_{\rm tot}$ eV	$R_{1,2;1,3}$ A	$R_{2,3}$ Å	$\angle 213^\circ$	ω (b ₂)cm ⁻¹	$\omega(a_1)$ cm ⁻¹	$\omega(a_1)$ cm ⁻¹
				${}^{11}A_1$ (19-5-7-13 16-2-6-10) Grid = FINE			
BPW91	$+0.011$	2.330	2.095	53.4	75	249	365
BLYP	0.0°	2.350	2.117	53.5	33	242	355
BP86	$+0.002$	2.323	2.091	53.5	66	251	367
BPBE	$+0.012$	2.328	2.093	53.4	76	250	365
PBEPBE	0.0°	2.328	2.099	53.6	65	252	364
PP86	0.077	2.339	2.103	53.4	54i	253	357
					${}^{11}A_1$ (19-5-7-13 16-2-6-10) Grid = UltraFINE		
BPW91	$+0.011$	2.329	2.094	53.4	70	247	365
BLYP	0.0°	2.350	2.117	53.5	16	239	353
BP86	$+0.001$	2.322	2.090	53.5	61	249	368
BPBE	$+0.010$	2.328	2.093	53.4	71	248	366
PBEPBE	0.0	2.327	2.099	53.6	60	250	364

^a The PP86 results are from ref 47. Total energy shifts (∆*E*) are given with respect to the lowest energy state obtained by the corresponding method and grid.

TABLE 4: 11B2 State of Fe3 Computed Using the BPW91, BLYP, BP86, BPBE, PBEPBE (Using Two Sample Grids for Integrating Exchange-Correlation Energy Contribution), and PP86 Levels*^a*

method	ΔE_{tot} eV	$R_{1,2;1,3}$ Å	$R_{2,3}$ Å	$\angle 213^\circ$	ω (b ₂)cm ⁻¹	$\omega(a_1)$ cm ⁻¹	$\omega(a_1)$ cm ⁻¹			
${}^{11}B_2$ (19-5-7-13 16-3-5-10) Grid = FINE										
BPW91	$+0.19$	2.259	2.225	59.0	193	347	1713			
BLYP	$+0.16$	2.279	2.247	59.1	1470i	187	334			
BP86	$+0.18$	2.251	2.222	59.1	195	350	1651			
BPBE	$+0.18$	2.256	2.224	59.1	194	347	1509			
PBEPBE	$+0.17$	2.256	2.231	59.3	199	346	1255			
PP86	$+0.22$	2.254	2.251	59.9	Not Computed					
					${}^{11}B_2$ (19-5-7-13 16-3-5-10) Grid = UltraFINE					
BPW91	$+0.19$	2.258	2.226	59.0	197	349	1527			
BLYP	$+0.16$	2.281	2.244	58.9	995i	190	337			
BP86	$+0.18$	2.250	2.224	59.1	199	352	1265			
BPBE	$+0.19$	2.256	2.225	59.1	198	350	1379			
PBEPBE	$+0.17$	2.255	2.232	59.3	204	349	1096			

^a The PP86 results are from ref 47. Total energy shifts (∆*E*) are given with respect to the lowest energy state obtained by the corresponding method and grid.

TABLE 5: 11B1 State of Fe3 Computed Using the BPW91, BLYP, BP86, BPBE, PBEPBE (Using Two Sample Grids for Integrating Exchange-Correlation Energy Contribution), and PP86 Levels*^a*

method	ΔE_{tot} eV	$R_{1,2;1,3}$ A	$R_{2,3}$ Å	$\angle 213^\circ$	ω (b ₂)cm ⁻¹	$\omega(a_1)$ cm ⁻¹	ω (a ₁) cm ⁻¹
				${}^{11}B_1$ (18-5-7-14 15-3-6-10) Grid = FINE			
BPW91	$+0.001$	2.208	2.353	64.4	50i	199	353
BLYP	$+0.002$	2.229	2.377	64.4	74	191	339
BP86	0.000	2.203	2.347	64.4	36	200	357
BPBE	0.000	2.207	2.349	64.3	57i	200	355
PBEPBE	0.000	2.211	2.353	64.3	32	201	352
PP86	$+0.004$	2.219	2.363	64.3	73	198	345
					${}^{11}B_1$ (18-5-7-14 15-3-6-10) Grid = UltraFINE		
BPW91	$+0.001$	2.210	2.353	64.4	63i	197	350
BLYP	$+0.001$	2.229	2.380	64.4	80	189	338
BP86	0.000	2.204	2.346	64.4	20i	198	353
BPBE	0.002	2.208	2.350	64.3	69i	198	351
PBEPBE	0.004	2.212	2.352	64.3	22i	199	349

^a The PP86 results are from ref 47. Total energy shifts (∆*E*) are given with respect to the lowest energy state obtained by the corresponding method and grid.

Fe₂ and Fe₃. Unlike Salahub and Chrétien,⁴⁷ we found all the states with the $Fe₂Fe₁Fe₃$ angles larger than 60 $^{\circ}$, including the $^{11}B_1$ state given in Table 5, to be transition states.

Comparison of Performance of LSDA, B3LYP, and DFT-GGA Levels. Because there are rather accurate experimental data for the EAs of iron clusters,^{15,16} it is interesting to compare the performance of different methods for Fe₃ and Fe₄, where the LSDA and DFT-GGA levels predict the ground states of different net spins. Computations were performed using the LSDA, B3LYP, BLYP, BP86, BPBE, PBEPBE, and BPW91 levels for the A' and A'' states of $Fe₃$ and $Fe₃⁻$ for 2S values of 8 and 10 for the neutral and 9 and 11 for the anion. (Because some of the functionals yield C_s symmetry, all of the results are given in this symmetry, even though most functionals yield C_{2v} symmetry). Computations on Fe₄ and Fe₄⁻ are performed
without any symmetry constraints for 2S values of 12 and 14 without any symmetry constraints for 2S values of 12 and 14 for the neutral and 13 and 15 for the anion. The initial guess orbitals in each optimization were taken from the corresponding BPW91 calculation. The results of calculations are presented in Tables 6-9 (frequencies and dipole moments) and Figures ²-5 (geometries and Mulliken atomic charges and open-shell occupation per atom in the anions and cations). The open-shell occupation is consistent with experimental measurements of local magnetic moments on atoms, because the magnetic

TABLE 6: Vibrational Frequencies, Dipole Moments, and Relative Total Energies of Two Candidates for the Ground State of Fe3 Computed at Different Levels $Fe₂ (2S+1 = 9)$

				Γ C3 (\angle Δ T Γ – γ)			
	LSDA	B3LYP BLYP		BP86		BPBE PBEPBE BPW91	
	9A "	9A''	9A''	9A''	9A''	9A''	9A''
ω_1 , cm ⁻¹	255	227	218	219	222	227	222
ω_2	255	229	218	221	224	228	223
ω_3	412	360	363	378	375	373	374
μ , Debye	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$\Delta E_{\rm tot}$, eV	0.0	$+1.25$	$+0.13$	$+0.17$	$+0.25$	$+0.22$	$+0.25$

 $Fe₃ (2S+1 = 11)$

						LSDA B3LYP BLYP BP86 BPBE PBEPBE BPW91	
	$11\,\mathrm{A}^{\prime}$	$11\,\mathrm{A}^{\prime}$	$11\,\mathrm{A}$	11 A $^{\prime\prime}$	11 A $^{\prime\prime}$	11Δ "	11_A "
ω_1 , cm ⁻¹	66	95	51	85	49	32.	62
ω	221	150	207	232	231	234	231
ω ₃	393	210	347	355	353	352	353
μ , Debye	0.47	0.61	0.56	0.74	0.78	0.75	0.78
ΔE_{tot} , eV +0.22		0.0	0.0	0.0	0.0	0.0	0.0

TABLE 7: Vibrational Frequencies and Total Energy Shift Relative to Those of the Corresponding Neutral Ground States of Fe3 - **Computed at Different Levels***^a*

^a The bold-font values correspond to the experimental EA of 1.43(6) taken with the opposite sign.

TABLE 8: Comparison of Vibrational Frequencies, Dipole Moments, and Relative Total Energy Shifts of Two Candidates for the Ground State of Fe4 Computed at Different Levels

	$Fe_4 (2S+1 = 13) C_1$										
	LSDA	B3LYP	BLYP	BP86	BPBE	PBEPBE	BPW91				
ω_1 , cm ⁻¹	181	43	146	153	152	155	152				
ω_2	193	100	156	162	161	165	161				
ω_3	196	136	168	184	186	185	186				
ω_4	196	160	168	185	187	185	187				
ω_5	306	199	265	279	278	279	278				
ω_6	409	269	358	373	370	369	371				
μ , Debye	0.00	1.05	0.00	0.00	0.00	0.00	0.00				
$\Delta E_{\rm tot}$, eV	0.0	$+0.50$	0.00	$+0.02$	$+0.09$	$+0.06$	$+0.08$				
	$Fe_4 (2S+1 = 15) C_1$										
	LSDA	B3LYP	BLYP	BP86	BPBE	PBEPBE	BPW91				
ω_1 , cm ⁻¹	128	119	93	104	105	106	104				
ω_2	141	128	113	125	125	128	125				
ω_3	256	151	202	207	201	208	200				
ω_4	261	164	202	207	201	208	201				
ω_5	262	215	220	230	229	231	228				
ω_6	394	266	332	351	347	347	347				
μ , Debye	0.00	0.05	0.00	0.00	0.00	0.00	0.00				
$\Delta E_{\rm tot}$, eV	$+0.30$	0.0	0.0	0.0	0.0	0.0	0.0				

moment is $\mu = g\mu_B S$ within the Heisenberg model (where g is close to 2.0, μ_B is Bohr magneton, and S is the spin operator). That is, the open-shell occupation is essentially gS.

As seen in Table 6, all methods predict the lowest state of Fe₃ with $2S = 8$ to be A'', while there is a competition between

TABLE 9: Comparison of Vibrational Frequencies and Total Ergies with Respect to Those of the Corresponding Ground State Neutrals of Fe4 - **Computed at Different Levels***^a*

	$Fe4- (2S+1 = 14) C1$										
	LSDA	B3LYP	BLYP	BP86	BPBE	PBEPBE	BPW91				
ω_1 , cm ⁻¹	176	52	137	144	141	147	141				
ω_2	191	99	158	162	162	166	162				
ω_3	221	142	191	200	177	203	199				
ω_4	223	144	192	202	211	209	202				
ω_5	244	188	197	212	229	217	210				
ω_6	395	256	341	357	354	355	354				
$\Delta E_{\rm tot}$, eV	-2.00	-1.11	-1.32	-1.58	-1.34	-1.41	-1.36				
			$Fe4- (2S+1 = 16) C1$								
	LSDA	B3LYP	BLYP	BP86	BPBE	PBEPBE	BPW91				
ω_1 , cm ⁻¹	154	147	75	75	53	79	81				
ω_2	181	181	102	93	99	82	82				
ω_3	230	186	122	129	131	133	129				
ω_4	264	187	176	184	185	187	183				
ω_5	264	240	195	204	206	206	205				
ω_6	381	296	324	340	340	340	340				
$\Delta E_{\rm tot}$, eV	-1.97	-1.81	-1.51	-1.88	-1.75	-1.77	-1.76				

^a The bold-font values correspond to the experimental EA of 1.78(6) taken with the opposite sign.

Figure 2. Bond lengths and Mulliken open-shell occupation per atom obtained for Fe₃ at different levels of theory.

the A' and A'' states for $2S = 10$. Only the LSDA level predicts $9A'$ as the lowest state; the geometry of this state is an equilateral triangle at all levels of theory. The B3LYP level has placed the $9A''$ state too high with respect to the $11A'$ state. At the LSDA, B3LYP, and BLYP levels, the ¹¹A' state is below the $11A''$ state, while the remaining methods predict the $11A''$ state to be the more stable of the two. As shown in Figure 2, the 11A " state is an isosceles triangle with the Fe₂Fe₁Fe₃ angle smaller than 60° , while the $^{11}A'$ state has an angle larger than

Figure 3. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for $Fe₃⁻$ at different levels of theory.

60°. It is interesting to note that the B3LYP and BLYP approaches predict a triangle with all bond lengths different.

The results of calculations on the $Fe₃⁻$ anion are less dependent on the choice of functional as shown in Table 7 and Figure 3. Excluding LSDA, all the levels yield a $^{10}A''$ ground state, which is appreciably below the $12A''$ state; the LSDA predicts the ground state to be $^{12}A'$. The geometry of the $^{12}A''$ state $(^{12}A'$, LSDA) is an equilateral triangle. As shown in Table 7, the adiabatic electron affinities computed at all levels are in rather good agreement with experiment. The largest discrepancy of 0.25(6) eV is obtained at the LSDA level. The best values are obtained at the BPBE, PBEPBE, and BPW91 levels, where the difference with experiment does not exceed 0.05(6) eV.

As shown in Table 8 and Figure 4, the performance of the BLYP, BP86, BPBE, PBEPBE, and BPW91 levels for Fe₄ is rather similar. All of them predict similar geometries (of D_{2h} shape), vibrational frequencies, and place the state with $2S =$ 14 slightly below the state with $2S = 12$. The B3LYP level predict distorted geometries and places the $2S = 12$ state well above the $2S = 14$ state. Only the LSDA predicts the $2S = 12$ state as the ground state, as found in the previous LSDA studies.

A similar trend is found for the $Fe₄⁻$ anion (see Table 9 and Figure 5). The B3LYP predicts geometries of the $2S = 13$ and $2S = 15$ in large variance with those obtained at the rest of the levels. The LSDA seems to underestimate some bond lengths by as much as 0.1 Å and predicts the $2S = 13$ state to be the lowest one. Again, the adiabatic electron affinities computed at all the levels are in good agreement with experiment. The largest deviations are obtained at the LSDA $[+0.22(6)$ eV] and BLYP [-0.27(6) eV] levels. The EAs obtained at the BPBE, PBEPBE, and BPW91 levels are in excellent agreement with experimental values.

BPW91 Results on the Fe*n***, Fe***n***-, and Fe***ⁿ* ⁺ **Clusters.** As found in the previous section, the Perdew's correlation func-

Figure 4. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for Fe4 at different levels of theory.

Figure 5. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for Fe₃⁻ at different levels of theory.

tionals yield very similar results that depend only marginally on the choice of the exchange functional (compare the BPBE

Figure 6. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for $Fe₃$, $Fe₃⁻$, and $Fe₃⁺$ obtained at the BPW91 level.

Figure 7. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for $Fe₄$, $Fe₄⁻$, and $Fe₄⁺$ obtained at the BPW91 level.

and PBEPBE results); therefore, the remaining computations were performed at the BPW91 level. Figures 6-9 show the geometries and Mulliken open-shell occupation per atom of the Fe_n, Fe_n⁻, and Fe_n⁺ clusters ($n = 3-6$), as well as the Mulliken
atomic charges in charged clusters. The atomic charges in neutral atomic charges in charged clusters. The atomic charges in neutral clusters are nearly zero and not shown in the figures. Vibrational frequencies and relative IR intensities of the ground-state clusters are given in Table 10.

Figure 8. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for Fe_5 , Fe_5^- , and Fe_5^+ obtained at the BPW91 level.

Figure 9. Bond lengths and Mulliken atomic charges and open-shell occupation per atom obtained for $Fe₆$, $Fe₆⁻$, and $Fe₆⁺$ obtained at the BPW91 level.

The ground state of $Fe₃$ ⁺ has $2S = 9$; one less than the ground
te of $Fe₂$, which is in agreement with a one-electron nature state of Fe3, which is in agreement with a one-electron nature of electron detachment process. The same holds for Fe_2^+ , Fe_5^+ , and Fe_6^+ , while Fe_4^+ is an exception, since its lowest energy state has $2S = 11$, in agreement with the previous theoretical

TABLE 10: Computed Vibrational Frequencies (cm-**1) and IR Relative Intensities (Arbitrary Units) of the Ground-State Fe***n***, Fe***ⁿ* -**, and Fe***ⁿ* ⁺ **Clusters***^a*

	ω_1	ω_2	ω_3	ω_4	ω_5	ω_6	ω_7	ω_8	ω ⁹	ω_{10}	ω_{11}	ω_{12}
Fe ₃	62 [1]	231 [0.05]	353 [0.00]									
Fe ₃	214 [0.40]	214 [1]	325 [0.09]									
$Fe3$ ⁺	125 [0.25]	143 [1]	328 [0.56]									
Fe ₄	104 [0.00]	125 [0.59]	200 [1]	201 [0.91]	228 [0.00]	345 [0.00]						
Fe ₄	81 [0.99]	81 [1]	129 [0.00]	183 [0.00]	205 [0.00]	340 [0.00]						
$Fe4$ ⁺	153 [0.00]	155 [0.00]	245 [0.97]	247 [1]	247 [1]	372 [0.00]						
Fe ₅	107 [0.02]	107 [0.01]	121 [1]	161 [0.53]	194 [0.00]	223 [0.55]	232 [0.07]	281 [0.03]	350 [0.17]			
Fe ₅	80 [0.02]	90 [0.02]	148 [0.04]	166 [0.05]	202 [0.00]	221 [0.01]	244 [0.03]	279 [1]	337 [0.01]			
$Fe5$ ⁺	74 [0.02]	123 [0.02]	153 [0.37]	158 [0.04]	179 [0.00]	220 [0.47]	248 [1]	275 [0.18]	352 [0.02]			
Fe ₆	53 [0.06]	116 [0.00]	148 [0.01]	151 [0.00]	163 [0.00]	175 [0.00]	205 [0.00]	235 [0.00]	245 [0.25]	256[1]	301 [0.42]	337 [0.00]
Fe ₆	86 [0.20]	99 [0.00]	144 [0.00]	148 [0.00]	173 [0.00]	180 [0.00]	202 [0.00]	207 [0.01]	257 [1]	265 [0.30]	295 [0.17]	336 [0.00]
$Fe6$ ⁺	65 [0.03]	105 [0.00]	150 [0.00]	152 [0.01]	177 [0.00]		197 [0.00] 212 [0.00]	216 [0.00]	233 [0.85]	259 [0.50]	269 [1]	320 [0.00]

a Absolute intensity ratios Neutral/Anion/Cation (each in km/mole); Fe₃, 36.44:0.02:1.86; Fe₄, 2.53:0.0012:3.31; Fe₅, 4.23:1.64:7.54; Fe₆, 3.09: 3.72: 3.94.

results.^{34,47} No such violation of the " \pm 1 rule" is found for the anions from Fe_2 ⁻ to Fe_6 ⁻. As was noticed before, $37,47$ the excited states of Fe₄ and its ions may have planar or near-planar geometrical configurations; we find planar structure for some excited states of the ions, see Figure 7.

As shown in Figure 8, the neutral and charged Fe₅ clusters in the ground and lowest excited states possess distorted *D*³*^h* geometries. The neutral ground state has $2S = 17$; a similar structure and the same net spin were found in the previous LSDA calculations.³⁴ However, the LSDA bond lengths³⁴ are shorter by \sim 0.1 Å with respect to those found at the DFT-GGA levels. No geometries were reported for either Fe_5 ⁻ or Fe_5 ⁺. Attachment or detachment of an electron results in changes of the bond lengths up to 0.08 Å without changing the geometrical shape (see Figure 8). The charges are nearly evenly distributed in Fe_5 ⁺, while two apex atoms of Fe_5 ⁻ have somewhat larger charges and smaller open-shell occupations.

The first ECP LSDA calculations³⁶ on the neutral Fe₆ cluster predicted a caped trigonal bipyramid. Subsequent LSDA calculations^{37,41} predicted a compressed D_{2h} distorted octahedron with $2S = 20$ for the ground state of Fe₆. The latter is in agreement with our computations (see Figure 9). However, there is a large difference in the bond lengths: the LSDA predicts⁴¹ the range of $2.29 - 2.53$ Å, while the BPW91 provides the range of 2.32-2.72 Å. Attachment or detachment of an electron does not seriously affect the bond lengths in the corresponding ground-state Fe_6 ⁻ and Fe_6 ⁺ ions. However, the charge distributions are different; in the anion, the charge is mostly localized on the rectangular base, while in the cation, it is localized on the apex atoms.

Vibrational Frequencies of the Fe_n , Fe_n^- , and Fe_n^+ **Clusters.** Harmonic vibrational frequencies computed for the ground state neutral and charged iron clusters are presented in Table 10. The frequencies are generally small; the smallest frequency of 53 cm⁻¹ belongs to Fe₆, while the largest frequency of 372 cm^{-1} belongs to Fe_4 ⁺. Many modes have rather small IR intensities. The modes of $Fe₃⁻$ and $Fe₄⁻$ possess especially low intensities (see footnote to Table 10).

The LSDA and DFT-GGA frequencies have been reported³⁴ for neutral Fe_n $(n = 2-5)$. For Fe₂, the LSDA and DFT-GGA frequencies are 497 cm⁻¹ and 474 cm⁻¹, respectively; for Fe₃, the frequencies are similar to our LSDA values for the ${}^{9}A''$ state given in Table 6 (the largest difference is less than 20 cm^{-1}), while the LSDA vibrational frequencies of Fe₄ are in a large variance with our LSDA frequencies presented in Table 8 for $2S = 12$ and are closer to those computed for $2S = 14$ (where the largest difference is 20 cm^{-1}).

Salahub and Chrétien 47 reported vibrational frequencies for the ground-state Fe_3 , Fe_3^+ , and Fe_4^+ clusters computed at the

TABLE 11: Comparison of Theoretical and Experimental Electron Affinities and Ionization Energies of Iron Clusters

	Fe ₂	Fe ₃	Fe ₄	Fe ₅	Fe ₆
			EA_{ad} , eV		
BPW91	0.94	1.47	1.76	1.84	1.61
LSDA ^a	0.95	1.37	1.69	2.08	
PP86 ^b	1.17	1.73	2.10		
$Expl^c$	$0.902(8)^{d}$	1.47(8)	1.72(8)	1.81(8)	1.51(8)
$Expl^e$		1.43(6)	1.78(6)	1.84(6)	1.58(6)
			IE_{ad} , eV		
BPW91	6.68	5.82	5.71	6.04	6.15
LSDA ^a	7.21	6.27	5.90	6.37	
$PP86^b$	7.14	6.28	6.20		
ExpV Expl ^g	6.30(1)	6.45(5)	6.4(1)	5.95(5) 6.20	5.9(1) 5.96
$Expl^h$			6.78(36)	6.30(12)	6.26(16)

^a Ref 34. *^b* Ref 47. *^c* Ref 15. *^d* Ref 12. *^e* Ref 16. *^f* Ref 17. *^g* Ref 18. *^h* Ref 19.

PP86 level. While our BPW91 frequencies given in Table 10 are close to theirs for Fe₃ (the largest difference is 6 cm⁻¹) and $Fe₄⁺$ (the largest difference is 26 cm⁻¹), for $Fe₃⁺$, they differ with our values by as much as 106 cm^{-1} . Our computed asymmetric stretching frequency of $Fe₃$ is in good agreement with the value of 180 cm^{-1} reported by Nour et al., ¹³ but as noted above, Moscovits and co-workers questioned this assignment. We note that for $Ni₃$, our computed⁷⁴ value differs from experiment¹³ by 20 cm⁻¹, suggesting that the Fe₃ asymmetric frequency, if not 180 cm^{-1} as assigned by Nour et al., is probably close to this value.

Electron Affinities and Ionization Energies. Computed adiabatic electron affinities (EA) and ionization energies (IE) are compared to experiment in Table 11. There is remarkably good agreement between the BPW91 EAs and most recent¹⁶ experimental values obtained by laser photodetachment spectroscopy. The largest discrepancy is only 0.03 eV, which is within the experimental uncertainty of ± 0.06 eV. Unexpectedly, the PP86 values differ from the experimental values to a larger extent than the LSDA values.

Laser photoionization has been used to determine the ionization thresholds, which probably correspond to vertical ionization energies (IEs). For Fe₂ and Fe₃, only one experimental study¹⁷ appears to have been published. For $Fe₄$ to $Fe₆$, there are more than one experimental values, and they show differences with each other of up to almost 0.4 eV, see Table 11. Our values, which are presented in Table 11, are adiabatic values. However, our computed vertical IEs show only small differences (less than 0.1 eV) with the adiabatic values, except for Fe₄, where the vertical IE to the cation ground state with $2S + 1 = 12$

TABLE 12: Theoretical (BPW91) and Experimental Fragmentation Energies of Neutral and Charged Iron Clusters

neutral			anion		cation		
channel	TW	exp ^a	channel	TW	channel	TW	$exp^{a,b}$
$Fe2 \rightarrow Fe + Fe$	2.18	1.18	$Fe^{-} \rightarrow Fe^{-} + Fe$	2.53	$Fe+ \rightarrow Fe+ + Fe$	3.35	2.78
$Fe_3 \rightarrow Fe_2 + Fe$	2.32	1.91	$Fe_3^- \rightarrow Fe_2 + Fe^-$	3.18	$\text{Fe}_{3}^{+} \rightarrow \text{Fe}_{2}^{+} + \text{Fe}$	3.17	1.75
			\rightarrow Fe ₂ ⁻⁺ Fe	3.84	\rightarrow Fe ₂ +Fe ⁺	4.34	3.20
$Fe4 \rightarrow Fe3+Fe$	3.06	2.19	$Fe4^- \rightarrow Fe3+Fe^-$	4.20	$Fe4+ \rightarrow Fe3+ + Fe$	3.13	2.28
\rightarrow Fe ₂ +Fe ₂	3.13		\rightarrow Fe ₃ ⁻ +Fe	3.34	\rightarrow Fe ₃ +Fe ⁺	5.14	
			\rightarrow Fe ₂ +Fe ₂ ⁻	4.00	\rightarrow Fe ₂ +Fe ₂ ⁺	4.11	2.50
$Fe5 \rightarrow Fe4+Fe$	3.26	2.25	$Fe^{-} \rightarrow Fe^{+}Fe^{-}$	4.54	$\text{Fe}_5^+ \rightarrow \text{Fe}_4^+ + \text{Fe}$	3.00	2.69
\rightarrow Fe ₃ +Fe ₂	4.17		\rightarrow Fe ₄ \rightarrow Fe ₄ \rightarrow Fe ₅	3.37	\rightarrow Fe ₄ +Fe ⁺	5.10	
			\rightarrow Fe ₃ +Fe ₂ ⁻	5.04	\rightarrow Fe ₂ +Fe ₃ ⁺	3.91	3.40
			\rightarrow Fe ₂ ⁻ +Fe ₂	4.52	\rightarrow Fe ₂ ⁺ +Fe ₃	4.79	3.20
$Fe6 \rightarrow Fe5+Fe$	3.74	3.17	$\text{Fe}_{6}^{-} \rightarrow \text{Fe}_{5} + \text{Fe}^{-}$	4.74	$\text{Fe}_{6}^{+} \rightarrow \text{Fe}_{5}^{+} + \text{Fe}$	3.57	3.26
\rightarrow Fe ₄ +Fe ₂	4.86		\rightarrow Fe ₅ ⁻ +Fe	3.51	\rightarrow Fe _s +Fe ⁺	5.36	
\rightarrow Fe ₃ +Fe ₃	5.57		\rightarrow Fe ₄ +Fe ₂ ⁻	5.52	\rightarrow Fe ₄ +Fe ₂ ⁺	5.33	
			\rightarrow Fe ₄ ⁻ +Fe ₂	4.69	\rightarrow Fe ₄ ⁺ +Fe ₂	4.38	
			\rightarrow Fe ₃ +Fe ₃ ⁻	5.71	\rightarrow Fe ₃ +Fe ₃ ⁺	5.18	

a Ref 25. For channels other than $Fe_n^+ \rightarrow Fe_{n-1}^+ + Fe$, the data are from ref 20.

(nonone-electron process) is 6.03 eV and to the cation state with $2S + 1 = 14$ is 6.21 eV. This latter value corresponds to a one-electron process and is much closer to the experiment. Our IEs for Fe₅ and Fe₆ are in good agreement with experiment. The largest (0.6 eV) discrepancy with experiment is found for the IE of Fe₃, assuming that the experimental IE for Fe4 corresponds to the computed vertical one-electron process.

Local Magnetic Moments of the Neutral Clusters. The Fe₂ bonding pattern shows that there is a $(4s + 4s)$ bonding orbital in each spin representation; the 3d spin-up electrons occupy localized atomic spin-orbitals and the 3d spin-down electrons occupy bonding orbitals. The local magnetic moments on atoms are defined by the difference in the number of their spin-up and spin-down electrons. Because the effective atomic 3d electronic configurations in the dimer are 3d7, the local magnetic moment on each Fe atom is 3μ **B**.

The NBO analysis shows that the bonding patterns in larger iron Fe_n clusters have similarities to those in $Fe₂$, but also show some significant differences. For all systems, the Fe atomic occupation is essentially $4s¹3d⁷$. Thus, the 3d electrons contribute $3\mu_B$ at all atomic sites. In Fe₂, both 4s electrons are in a bonding $(4s + 4s)$ orbital, and therefore do not contribute to the local magnetic moment. This is not true of the larger clusters, where some of 4s electrons occupy open-shell orbitals and therefore contribute to the local magnetic moment. We should note that "4s" orbitals actually show some mixing with the 3d orbitals and the NBO analysis shows that this hybridization increases from Fe₃ to Fe₆. While this mixing does not significantly affect the results for clusters containing up to six Fe atoms, it could become important for larger clusters.

In the $^{11}A_2$ ground state of Fe₃, the atomic occupation of the apex atom is $4s^{1.33}3d^{6.79}4p^{0.06}$, while those of the base atoms are $4s^{0.90}3d^{6.93}4p^{0.06}$. The three 4s electrons occupy one twoelectron bond and one one-electron spin-up bond, thus the 4s electrons contribute to the local magnetic moment, which is now larger than found for Fe₂, namely $3.7\mu_B$ and $3.2\mu_B$ on the apex and basal atoms, respectively (see Figure 6).

All four atoms of ground-state Fe₄ have the same effective atomic occupation $(4s^{1.07}3d^{6.85}4p^{0.07})$. The four 4s electrons occupy one two-electron bond and two one-electron bonds and therefore contribute $2\mu_B$ to the total magnetic moment. Because the 4s electrons are evenly distributed on the Fe atoms, the local magnetic moments is $3.5\mu_B$ on each Fe atom. In Fe₅, the 4s electrons occupy two two-electron bonds and one one-electron

bond, thus contributing 1μ **B** to the total magnetic moment. Due to its C_{2v} symmetry, Fe₅ possesses three types of atoms, see Figure 8. They have occupations and local magnetic moments of $4s^{0.60}3d^{7.04}4p^{0.09}$ and $2.9\mu_{\text{B}}$, $4s^{1.05}3d^{6.90}4p^{0.07}$ and $3.3\mu_{\text{B}}$, and $4s^{1.20}3d^{6.83}4p^{0.05}$ and 3.2μ **B**. Clearly, the open-shell 4s electron is not evenly distributed among the Fe atoms.

In Fe₆, the apex and basal atoms have occupation of $4s^{1.03}$ - $3d^{6.94}4p^{0.08}$ and $4s^{1.03}3d^{6.86}4p^{0.06}$, respectively. With four spinup and two spin-down 4s electrons, the 4s electrons contribute 2μ **B** to the total magnetic moment. Thus, the local magnetic moments of $Fe₃$ to $Fe₆$ are, on the average, larger than that found for $Fe₂$ due to contributions from the 4s electron. For $Fe₄$ and Fe6, a spin pairing of the 4s electrons could have occurred which would have resulted in the same local magnetic moment as in Fe2. Clearly, changes in the bonding must occur for larger clusters that to lead to a reduction in the local magnetic moment. Perhaps additional 4s to 3d promotion or 4s3d hybridization occurs, so that the "4s" one-electron bonds begin to appear in the spin down representation so that they reduce the magnetic moment rather than increase it.

Thermodynamic Stability. Fragmentation energies of positively charged iron clusters have been obtained $2⁰$ from collision induced-dissociation experiments, while the neutral cluster bond rupture energies (Fe $_{n-1}$ -Fe) were estimated²⁵ from the cation CID data and the experimental IEs. The recommended^{23,25} values of fragmentation energies are compared with our values computed at the BPW91 level in Table 12.

At the first glance, the theory overestimates the fragmentation energy by about 1 eV. It is known (see, e. g., ref 75) that the present DFT methods do not accurately describe the $5D(4s^2 3d⁶$) ground state of Fe atom, but in fact yield an occupation that is a mixture of $4s²3d⁶$ and $4s¹3d⁷$. This problem with the description of the Fe atom could be part of the reason for overestimating the bond rupture energies. For the neutral clusters, an additional source of error could be due to the differences in computed and experimental IEs, which have been used for deducing the bond rupture energies. Despite the overestimation of the bond energies, theory reproduces the experimentally observed trend of a general increase in the thermodynamic stability with increasing cluster size.

Conclusion

Our calculations on $Fe₃$, $Fe₄$, $Fe₃⁻$, and $Fe₄⁻$ suggest that one should avoid using the LSDA, B3LYP, and BLYP approaches when studying the structure of iron clusters. The Perdew family of correlation functionals provides similar structures and electronic properties. The use of the Becke or the Perdew-Burke-Ernzerhof exchange functionals yields essentially the same results as comparison of the BPBE or PBEPBE results show. The BPW91, BPBE, and PBEPBE approaches provide nearly the same values for the bond lengths, the vibrational frequencies, and the electron affinities. The latter are in remarkably good agreement with experiment. The BP86 level provides somewhat worse agreement with experiment. High local magnetic moments at iron sites are related to a specific type of chemical bonding in iron clusters. Effective atomic occupation is $(4s^{1+/-\delta}3d^{7-/-\delta})$ where δ is generally small. The 3d electrons contribute $3\mu_B$ per atom. The 4s electrons are not all paired in two-electron bonds, and therefore they also contribute to the magnetic moment. For the cluster sizes considered, we do not see a strong indication of a decreasing magnetic moment with cluster size. However, there is an increase in the 4s3d hybridization with cluster size, which leads us to speculate that as the cluster size increases, eventually either additional 4s to 3d promotion, or more likely, increased hybridization, will lead to an increase in the spin-down occupation at the expense of the spin-up occupation, resulting in a decrease in the local magnetic moment. In agreement with experiment, thermodynamic stability increases when moving from $Fe₂$ to $Fe₆$.

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